## **Objective Analysis**

<u>Definition:</u> **Objective Analysis** - A procedure for obtaining estimates of fields on a regular grid from irregularlyspaced values (typically observations).

This is usually in 2-D or 3-D space but could be in time.

## Cressman Objective Analysis Method (Cressman, 1959, MWR)

Cressman objective analysis obtain values at grid points,  $Z_{ij}^{a}$  (where *i* and *j* are the grid point indices for a 2D grid) as the weighted average of the difference between observed values  $Z_{k}^{o}$  and background values interpolated to the observation locations  $Z_{k}^{b}$  (i.e.,  $Z_{k}^{o} - Z_{k}^{b}$ , which is called observation increment) plus the background value at the grid point  $Z_{ij}^{b}$ .

$$Z_{ij}^{a} = Z_{ij}^{b} + \frac{\sum_{k} w_{k}(Z_{k}^{o} - Z_{k}^{b})}{\sum_{k} w_{k}}, \quad w_{k} = \frac{R^{2} - r_{k}^{2}}{R^{2} + r_{k}^{2}} \text{ for } r_{k} \le R.$$
(1)

The weight  $w_k$  is a function of the distance  $r = \sqrt{(x_{ij} - x_k)^2 + (y_{ij} - y_k)^2}$  is that between the individual observation k and grid point (i, j). R is the influence radius. Beyond the influence radius the weight is set to zero. R is therefore often referred to as cut off radius. The weight function  $w_k$  has the following shape as a function of radial distance r:



FIGURE 3.—Curve of the weighting function W vs. distance d. Solid line refers to equation (2). Dashed line refers to recent changes for scan 4 (see text).

R should not be too large or too small, and is usually chosen to be a few times of the average station separation distance.